

## SLO - A Program for Stope Limit Optimisation Using A Heuristic Algorithm

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**ABSTRACT:** The heuristic "Maximum Value Neighbourhood" (MVN) algorithm is proposed to optimise stope boundaries. The algorithm provides a 3D analysis and can be applied to any underground mining method. The MVN algorithm uses a 3D economic block model to locate the best neighbourhood of a block, which guarantees the maximum net value. Neighbourhoods are restricted by the mine geometry constraints. A Fortran 90 program, the "Stope Limit Optimiser" (SLO), has been developed to implement the algorithm. SLO integrates the Fortran 90 code of the algorithm with the Winteracter user interface features, to provide a Windows based interactive environment for defining the model specifications, stope constraints and mine economic factors and displaying the results as 2D plans/sections in a text mode view. Intermediate results are reported for each block and an on screen summary report is provided.

### 1 INTRODUCTION

Few algorithms have been developed for optimisation of the ultimate stope boundaries. The latest one, termed "Maximum Value Neighbourhood" (MVN), is based on a heuristic approach and benefits from its generality and simplicity (Ataee-pour & Baafi 1999). Few alternatives have been reported for the MVN algorithm including the Floating Slope Algorithm of Datamine (Alford 1995) and the Branch and Bound Technique (Ovanic and Young 1995). The MVN algorithm is implemented on a 3D economic block model, in which the problem of determining the best combination of blocks (for mining) that provides the maximum profit is formulated by Equation (1).

$$\left. \begin{array}{l} \text{Objective function :} \\ \text{Maximise } SEV = \sum_{jk} F_{jk} BEV_{jk} \\ \text{subject to :} \\ \text{slope geometry constraints} \end{array} \right\} \quad (1)$$

where

SEV: total stope economic value,

BEV<sub>jk</sub>: the economic value of the block, B<sub>jk</sub>.

F<sub>jk</sub>: an indicator function showing whether the block, B<sub>jk</sub> is mined or not. It is defined by Equation (2).

$$F_{ijk} = \begin{cases} 1 & \text{if } B_{ijk} \text{ is mined,} \\ 0 & \text{otherwise.} \end{cases} \quad (2)$$

Stope geometry constraint is formulated by the neighbourhood (NB) concept, which is based on the number of mining blocks equivalent to the minimum stope size. The size of the NB in terms of the number of blocks is defined as the order of neighbourhood (O<sub>jk</sub>). The MVN algorithm constructs the set of possible neighbourhoods for each block, calculates the dollar value of each NB, locates the NB with the maximum dollar value (MVN) and flags the corresponding blocks for inclusion in the final stope. The MVN algorithm has been implemented on small sized examples, using Excel Visual Basic modules (Ataee-pour and Baafi 2000).

An application program, the "Stope Limit Optimiser" (SLO) was developed to implement the MVN algorithm on actual mine data. SLO integrates Fortran W code of the algorithm with Winteracter user interface features. This paper introduces the procedure, capabilities and limitations of SLO and illustrates how a project is manipulated in SLO and how the optimisation results are displayed.

### 2 GENERAL PROCEDURE

SLO considers jobs for optimisation as projects. A project is a collection of input files that specify the

block model parameters, slope geometry constraints and economic factors. An interactive environment is provided for the user to define projects and import block data for the optimisation process. Figure 1 shows the *SLO* welcome page with the main menu. Using the "Project" option of the menu, the user may create a new project or open an existing one, save the project and close it or exit from the *SLO* application.

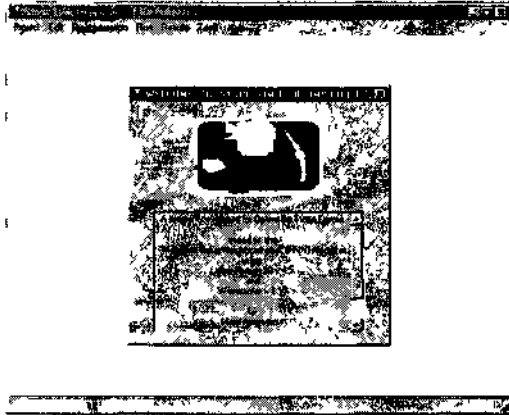


Figure 1 The *SLO* welcome page

The general performance of the *SLO* optimiser, for any project, is divided into three stages, i.e. the input, optimisation and output stages, as shown in Figure 2. During the input stage, all input data, including the block model definition, slope constraints, economic factors and the block data are edited and prepared using the "Edit" option. Each input data type is saved in a separate file for further use. In cases where block data contain only grade values, block economic values (*BEV*) are calculated from grade values by *SLO* through the data preparation phase of the "Preoptimisation" option. The final product of the input stage, however, is an economic-block model (a 3D array containing the economic values of the blocks) together with the 3D order of neighbourhood.

The optimisation stage is the core of the whole program. Optimisation may be performed on the whole, or a sub-region of, the block model. Using the "Preoptimisation" and "Run" options, a (sub) region is specified, the corresponding block data are imported and optimisation is performed in accordance with the order of neighbourhood and based on the *MVN* algorithm. The optimisation stage receives the 3D array of block economic values, as well as the order of neighbourhood, and produces a 3D array of block flag data.

The output stage includes all processes concerning the visualisation of the optimisation results (using the "Results" option). At this stage, *SLO* re-

ceives the 3D array of block flag data, arranges them in a plan or section order, wraps them in a table format with suitable annotations and finally displays the optimised slope layout in an ascx formatted file. Alternatively, the *SLO* exports the flag data directly into an ascx formatted file, accessible to other computer packages, which have been developed for 2D and 3D display of results. The output stage also includes the display of all the reports and intermediate results collected throughout the optimisation stage.

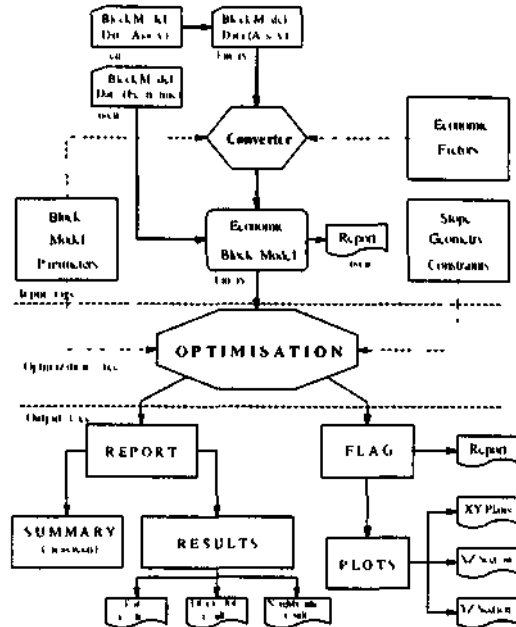


Figure 2 General scheme of the *SLO* flow-chart

### 3 PROJECT MANIPULATION

Projects are created, modified or deleted via three groups of files, i.e. model parameters files, slope constraints files and economic factors files.

#### 3.1 Block Model Definition

The model parameters files contain information about the specifications of the block model. These include the co-ordinates of the origin and the maximum limit of the block model, the extension and the number of the blocks in X, Y and Z directions, as well as the definition of possible sub-regions within the whole model. Figure 3 shows the main dialog box for the definition of the block model.

Block models may be defined in either the XYZ or UK mode. In the XYZ mode, the model co-ordinates and the block dimensions are entered by the user. The block volume, the number of blocks in

each direction and the total number of blocks within the model are automatically calculated. The UK mode requires that the user enter the number of blocks as well as the block's extensions in X, Y and Z dimensions. Then *SLO* calculates the minimum and maximum co-ordinates of the block model.

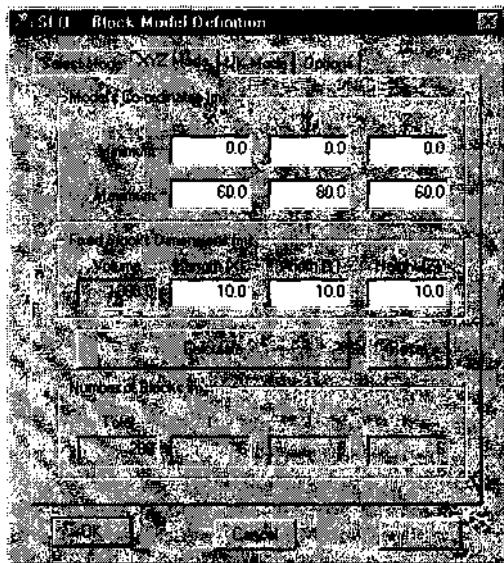


Figure 3. Defining the block model (XYZ mode)

It may be necessary to divide the block model due to geo-technical factors, different rock types or various mining methods. These impose different stope constraints to different parts of the block model. If this were to happen, various sub-regions may be defined to handle a variety of stope constraints and *orders of neighbourhood* within the model. When a deposit is too large and separate zones of mineralisation can be distinguished within the entire deposit, definition of various sub-regions may be helpful. In addition, the block model may contain either grade or economic values. *SLO* provides options to define both data types to a project. If economic values are used, the block data are directly used in optimisation. In cases where assay data are used, they should be converted into economic data before optimisation is performed. Through the "Options" sub-dialog in Figure 3, the user can state whether or not there are any sub-regions within the block model and specify the block data type.

### 3.2 Definition of the Stope Geometry Constraints

Information about the stope geometry constraints is collected in a separate file. The user should enter the minimum stope size, in terms of meters, for each of the three orthogonal directions. The stope block ra-

tio (*SBR*) and the *order of neighbourhood* ( $O_{,n}$ ), in each direction, is then calculated by *SLO*, based on the block size and the minimum stope size.  $O_{nh}$  is finally expressed in terms of the integer numbers, i.e. the number of blocks inside the minimum stope size in the X, Y and Z directions, respectively. The product of these three values indicates the total number of blocks within the minimum stope. It also indicates the total number of possible neighbourhoods for each block.

It is possible to define the stope constraints for the whole and/or sub-regions of the model. The existence of sub-regions often shows that there is not a consistent stope geometry constraint within the block model, so the constraints cannot be defined for the entire model but rather they should be defined for every sub-region. If the division of the model into sub-regions is not due to various stope constraints (e.g. it is because of a large deposit), then the stope constraints could be the same for all the sub-regions as well as for the entire model. This means that defining the stope constraints for sub-regions is not useful, unless the user is interested in performing the optimisation algorithm for a specified zone, instead of the entire model. *SLO* provides options to perform both cases. Figure 4 shows defining the slope constraints for a sub-region.

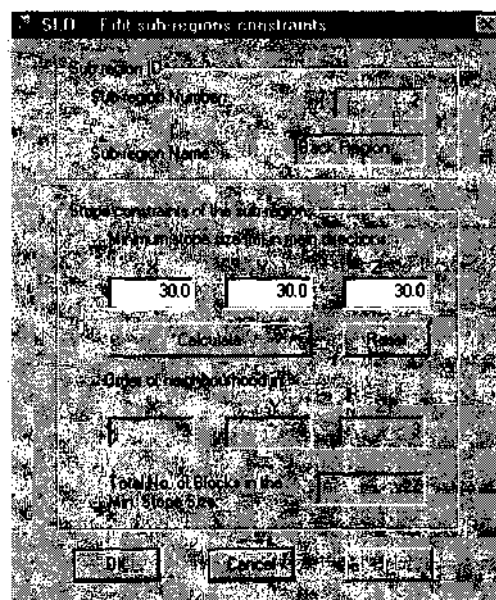


Figure 4. Defining the stope constraints (sub-regions)

### 3.3 Economic Factors

Another input to the system is information in respect of the economic parameters, which apply to mining the deposit. This information is used to help trans-

load assay data into the dollar value of the blocks. The required economic parameters include information about the products of mining, their prices, grades and price units, costs of mining/processing of the products, rates of recovery applied to products and the densities of the ore/waste. Figure 5 shows the economic parameters dialog box through which products of the deposit may be defined. Currently, *SLO* supports processing of economic factors for multi-product deposits containing up to four by-products.

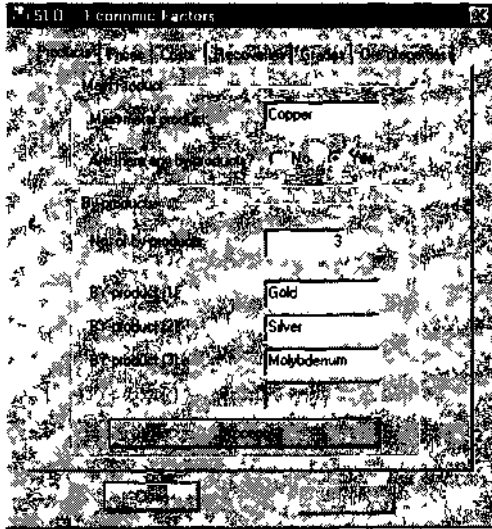


Figure 5 Defining the mine products

The price and the price unit of each product are required. The user may enter the price directly in a real field in the supplied dialog box. A list of three price units is available to select via a drop-down menu which include dollar per tonne, dollar per ounce and cents per kilo. Figure 6 shows the corresponding dialog box in *SLO*.

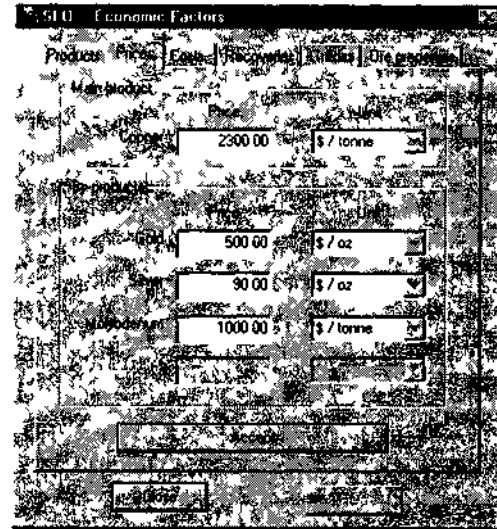


Figure 6 Defining prices and price units

There are two categories of costing applied in the optimisation of stope boundaries, i.e. ore-based costs and metal-based costs. Ore-based costs consist of all expenditures spent to extract the rock from the mine regardless of whether it is ore or waste. In order to obtain ore-based costs, all mining processes including preparation, drilling, blasting or haulage, should be considered. Then the average cost for mining one tonne of rock (ore or waste) forms the ore-based costs. Metal-based costs include all expenditures to recover the metal product from the mined ore. Obtaining costs for this category is by calculating the average cost for one tonne of the main product rather than the ore. The metal-based costs may be broken down into a number of components such as, the cost of smelting or processing, the cost of leaching, administration costs and other miscellaneous costs. The user may enter these cost information through a dialog shown in Figure 7.

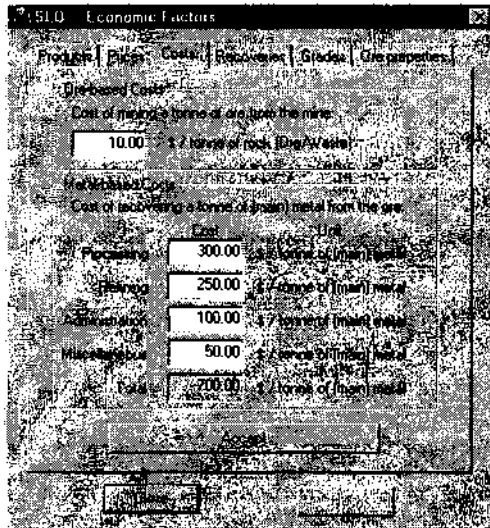


Figure 7. Defining various costs

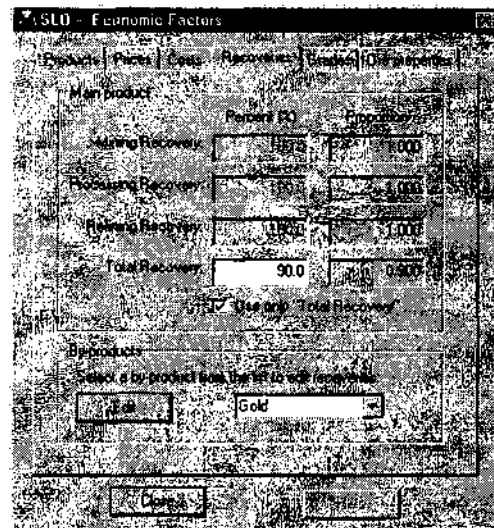


Figure 8. Defining various rates of recovery

*SLO* provides definition of recovery of the metal contents in three stages, i.e. the mining, processing (smelting) and the refining stage. The user enters the rate of recovery at each stage, in terms of percentage, and *SLO* returns the total rate of recovery. However, the user may enter directly the total rate of recovery, if available, and ignore the sub recoveries. Figure 8 shows the dialog box for defining the various rates of recovery. If there are any by-products, the rates of recovery should be defined for each by-product using an additional dialog box.

The grade values are entered via the assay data file, however, the units of grades are defined through the project files. The grade units are defined for each by-product as well as the main product. A list of two items is available for the selection of grade units, i.e. the percentage (%) and grams per tonne (ppm). Ore properties are the last economic factor described in the project file. In order to obtain the weight of a block, the specific gravity of the rock is needed. Two distinct categories of density, i.e. the density of the ore and the density of the waste are supported. A cut-off grade should be defined for the main product to discriminate between the ore and the waste. Figure 9 shows the *SLO* dialog box for defining the ore properties.

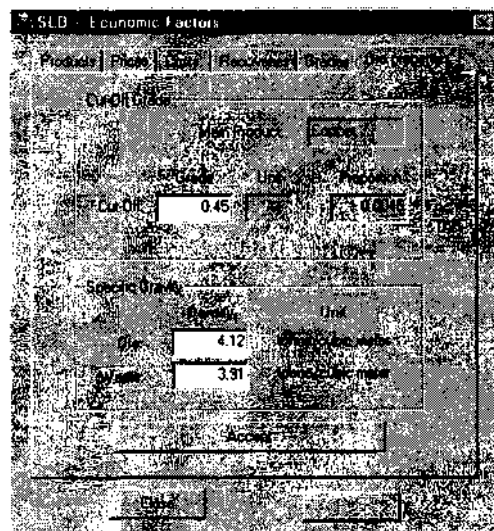


Figure 9. Defining ore properties

#### 4 BLOCK DATA FILE

The main block inputs to the optimiser is the economic values of blocks stored in a data file. In cases, where economic values are not available, the data file may include the assay data of blocks. In either case, data files must contain information about the address and value of each block. For economic data files, the block value is a real number that represents the estimate of the dollar value of that block. Where the input is assay data, the block value consists of a group of, up to five, real numbers, which represent

the estimated grade of the main product, as well as that of a maximum of four possible by-products for that block. It is possible for the user to view and edit the data files in ascn format before performing optimisation.

In multi-product projects where there are multiple grade values for each block, they are replaced by a single equivalent grade value, based on the main product grade. In order to calculate the equivalent grade value, the prices, grades and rates of recovery for each individual product are taken into consideration.

## 5 OPTIMISATION AND RESULTS

After all data are input in the required form, the user may choose the entire model or select a sub-region to perform optimisation. All required data corresponding to the blocks within the selected region are then imported and optimisation is performed based on the MVN algorithm. Finally, blocks of the optimised slope are flagged. The flag data of blocks are stored in an output file.

### 5 / Plots

The output file may be imported into other mine planning packages to display the end results in 2D and 3D views. However, SLO provides utilities for the user to produce and view the plots of the opti-

mate slope boundaries. The user may select the plotting of any of the 2D views of the slope including X-Y plans, X-Z sections and Y-Z sections, or all of the plots. It is also possible to specify a certain plan section, or a range of plans or sections of the optimised slope for plotting. Figure 10 shows the SLO dialog box for specifying plans, or sections, of the optimised slope to be plotted.

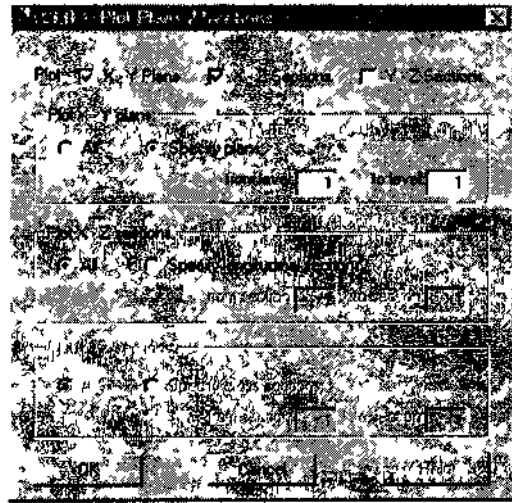


Figure 10 Specifying plans/sections to plot

PLAN h 12

	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	
29	*	0	0	0	0	0	0	0	0	0	1	1	1	1	1	1	1	1	1	0
28	*	0	0	0	0	0	0	0	0	0	1	1	1	1	1	1	1	1	1	0
27	*	0	0	0	0	0	0	0	0	0	1	1	1	1	1	1	1	1	1	0
26	*	0	0	0	0	0	0	0	0	0	1	1	1	1	1	1	1	1	1	0
25	*	0	0	0	0	0	0	0	0	1	1	1	1	1	1	1	1	1	1	0
24	*	0	0	0	0	0	0	0	0	1	1	1	1	1	1	1	1	1	1	0
23	-	0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0
22	*	0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0
21	>>	0	0	0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	0
20	*	0	0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0
19	*	0	0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0
18	*	0	0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0
17	*	0	0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0
16	*	0	0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0
15	*	0	0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0
14	*	0	0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0
13	*	0	0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0
12	*	0	0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0
11	*	0	0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0
10	*	0	0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0
9	*	0	0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0
8	*	0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0
7	*	0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0
6	*	0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0
5	*	0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0
4	*	0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0
3	*	0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0
2	*	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
1	*	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	*	*	*	*	*	*	*	*	*	*	*	*	*	*	*	*	*	*	*	*
	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	

Figure 11 An example of the plans/sections plotted in SLO

An example of such plotted plans/sections is shown in Figure 11. Currently, the plots of *SLO* are in text mode. It is envisaged to modify the application to plot in graphics mode.

### 5.2 Results Files

*SLO* reports the information obtained for the optimised blocks at each stage. This information is updated as the optimisation progresses and is finally saved in some report files. These include reports on the intermediate results, the neighbourhood results and a final on-screen summary report. Information about the set of possible neighbourhoods of each block and their dollar values are saved in the specified file. The intermediate results obtained for each block contain the *neighbourhood (NB)* number within the set of neighbourhoods of that block, which provides the maximum value, the maximum neighbourhood value, the marginal value obtained from the *MVN* of the block, and finally the updated stope value. These results obtained during the optimisation will help the user to see the variation of the stope after the optimiser examines each block.

### 5.3 Summary Report

After the optimisation is completed, a summary report of the optimisation results is provided and appended to the end of the intermediate results file. The summary report includes information such as the total number of blocks within the region, number of negative and non-negative valued blocks in the region, number of negative valued blocks included in the final stope, and then total values, number of non-negative valued blocks excluded from the final stope and their total values, total stope value, and the percentage of the block values included in the ultimate stope. Figure 12 shows a typical on-screen summary report.

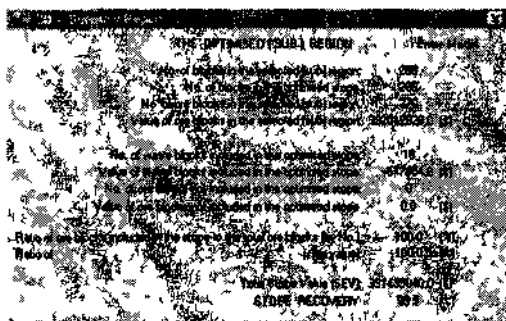


Figure 12. A typical on-screen summary report.

## 6 CONCLUDING REMARKS

*SLO* is a Windows based application program which may be used to interactively optimise stope boundaries, implementing the *MVN* algorithm. The major options available in *SLO* include XYZ and UK modes, defining sub-regions, accepting assay/economic value modes and supporting multi-product deposits (up to four by-products). It is possible to produce nested stopes by changing the economic parameters such as prices, costs, recoveries and cut-off grades and multiple running of *SLO*. This parameterisation is helpful in any decision making about the ore deposit including the feasibility study, preliminary mine evaluation and the mine closure. The variation in stope geometry constraints may also produce nested stopes which may help in mining method selection since different mining methods impose different stope geometry constraints. Running *SLO* for alternative mining methods will help in the selection of the method with the highest stope net value.

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